

# OUTLINE

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3. Deconvolution
4. Algorithm
5. Synthetic Aperture Sonar
6. SBIR Program Steps  
through the APB Process

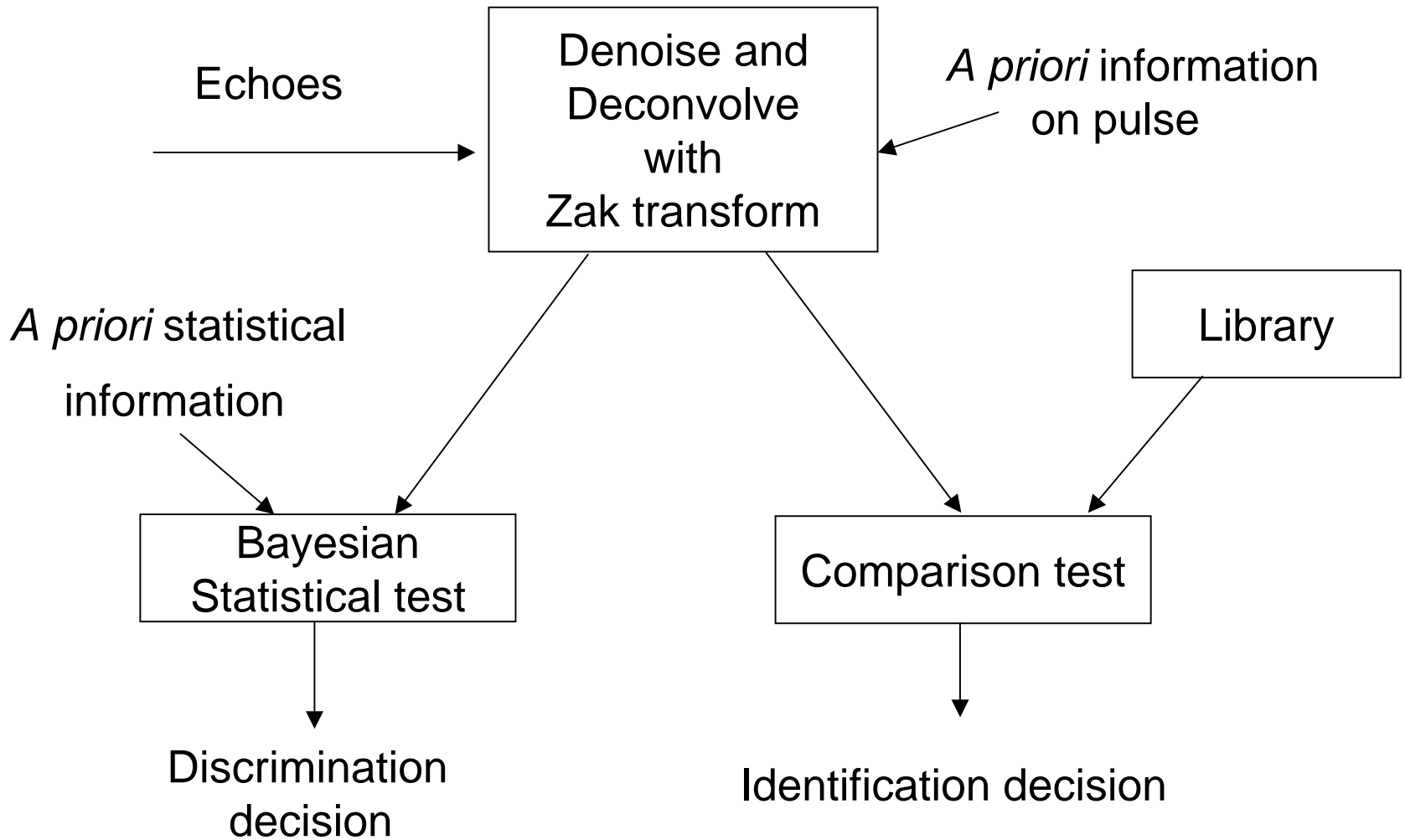


# THE MISAS APPROACH IS TO

- ✓ Exploit the ability of the ZAK transform to highly resolve an echo in time
- ✓ Use this capability to deconvolve an acoustic echo
- ✓ Increase observability with SAS



# MISAS Subsystem Process Diagram

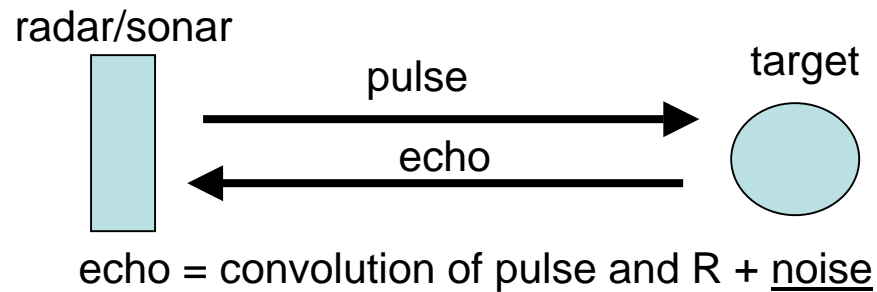


# TECHNOLOGY BACKGROUND



# Reflectivity Kernel Estimation

**Material properties  
of target summarized in  
reflectivity kernel  $R(t)$**

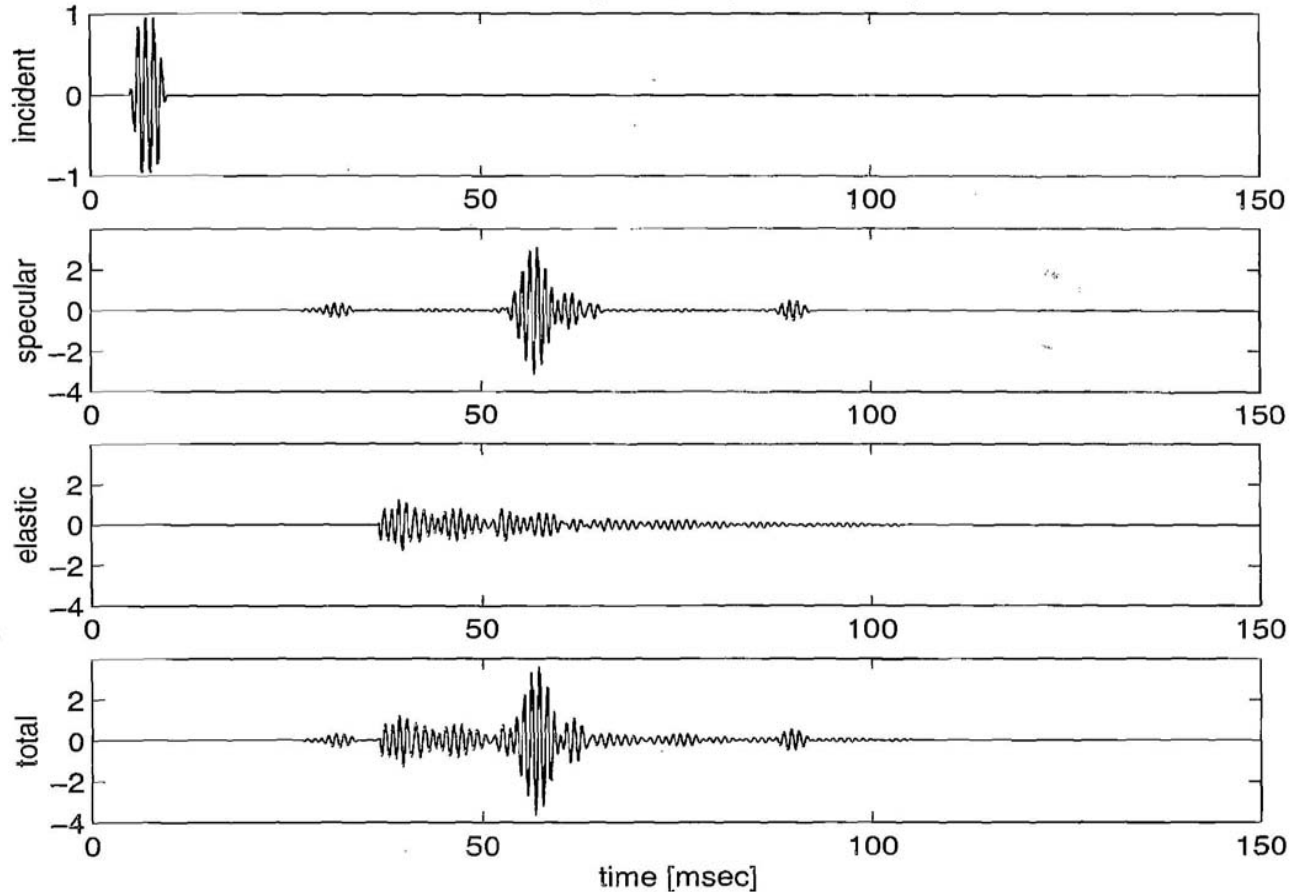


**Goal: Recover material information from noisy echo  
through deconvolution**



# Echo response for a 1.0kHz 5.0msec CW pulse

elevation = 0 degrees, aspect = 40 degrees



**Incident  
Pulse**

**Reflected Part  
of Echo**

**Reradiated  
Part of Echo**

**Total Echo**

Courtesy of Naval Undersea Warfare Center – Division, Newport,  
Code 8133 (15 November 2007)



# DECONVOLUTION



# Deconvolution

Given the input or “probe” signal, find the Kernel,  $K$ , from the received or scattered signal.  $K$  characterizes the material

This is an inverse problem. The associated forward problem is: Given  $K$  and an input signal  $s$ , find the scattered or output signal

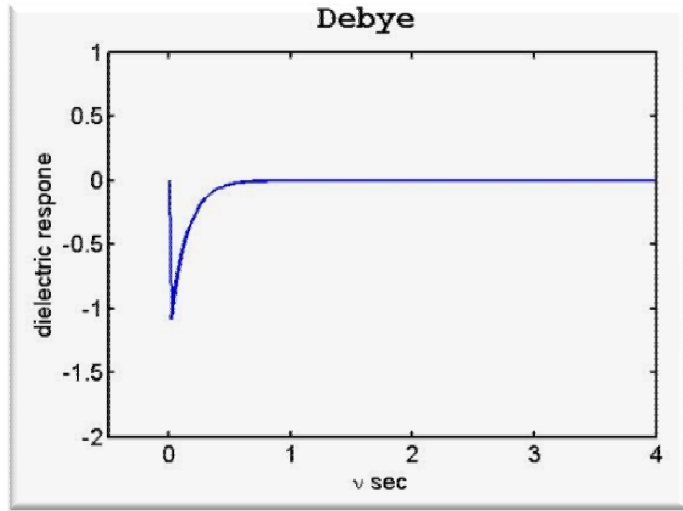
$$f(t) = \int K(t, t') s(t') dx' + noise$$

Output                      Kernel                      Input

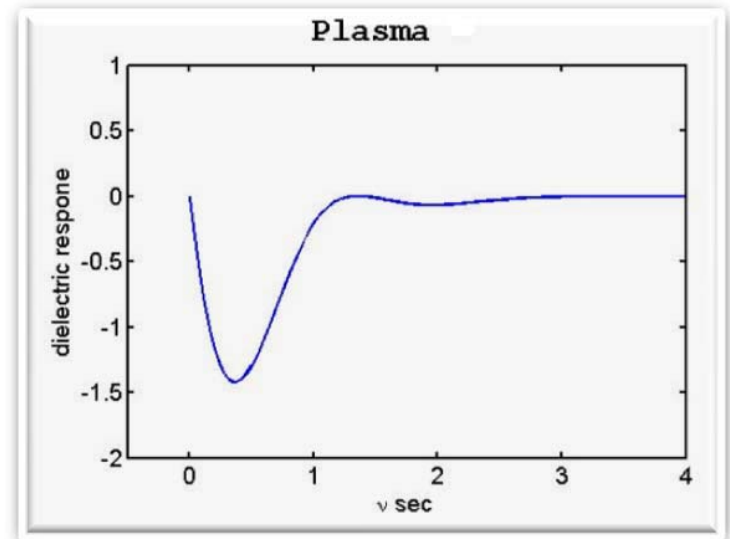
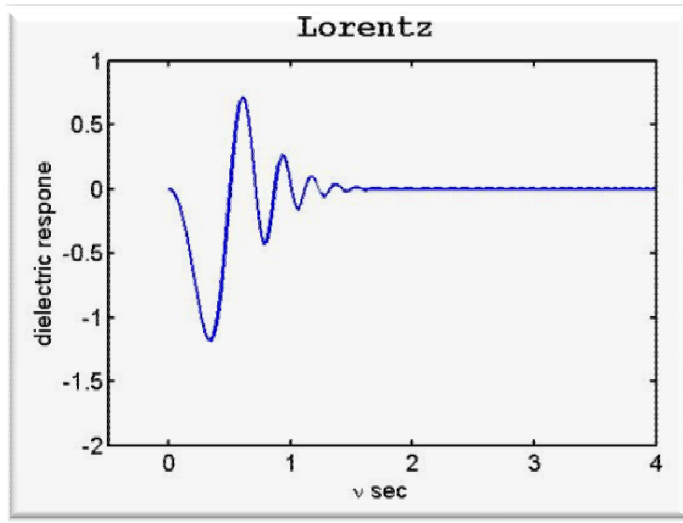




# Examples of Reflectivity Kernels



- Water
- Biological tissue
- Radar-absorbing urethane foam



- Atmospheric interference

- Heavy metals
- Composite materials



# ALGORITHM



# Based on the Zak Transform

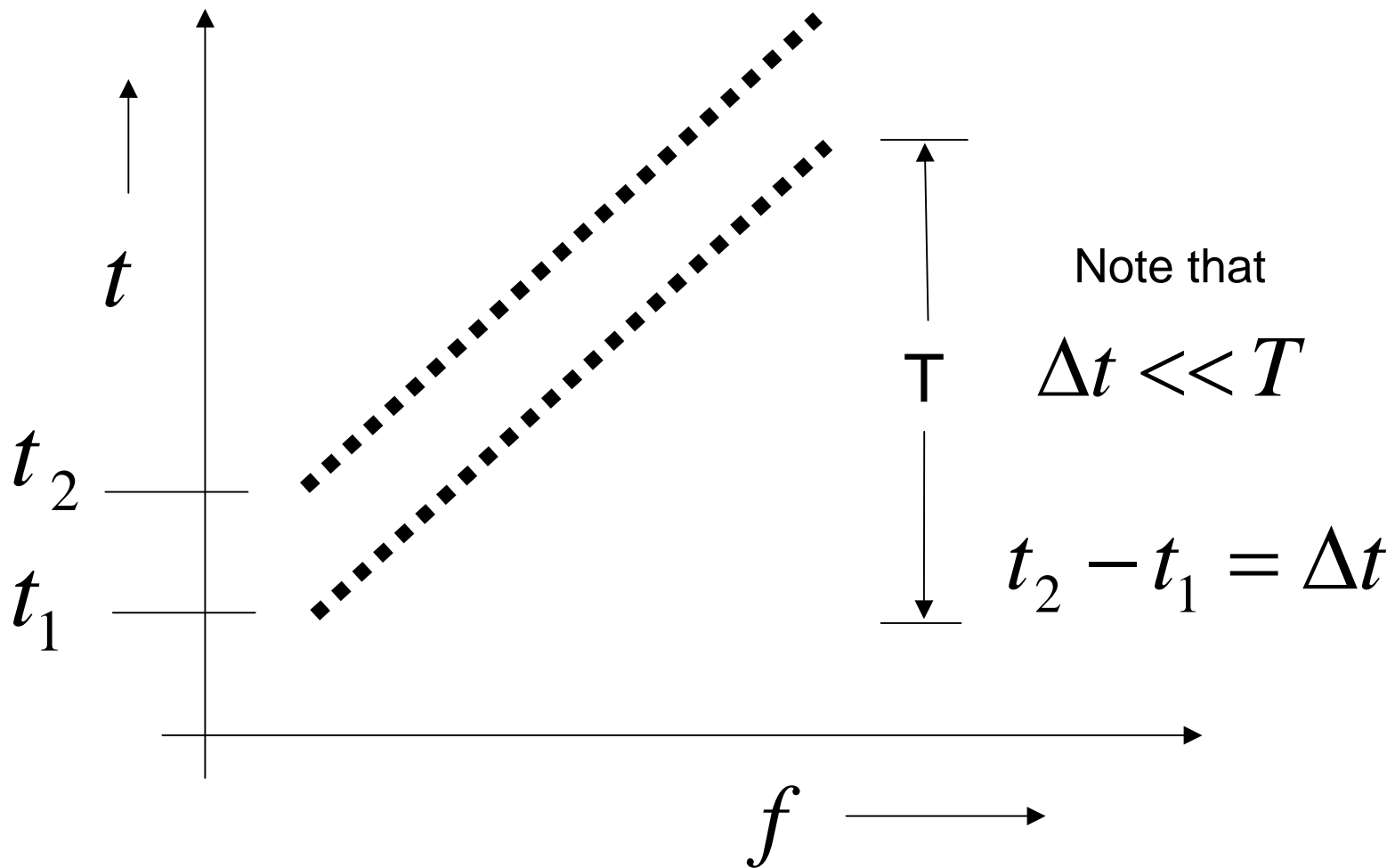
Fourier Transform  $f_n = \sum_{k=-\infty}^{+\infty} s(k) e^{-i2\pi \frac{nk}{N}}$

Zak Transform  $Z(t_m, f_n) = \sum_{k=-\infty}^{+\infty} s(t_m + k) e^{-i2\pi k f_n}$

The Zak transform is a time-frequency representation. It is more general than the Fourier transform In that it allows a great deal of flexibility in sampling



# Zak time-frequency map for 2 chirps at critical sampling



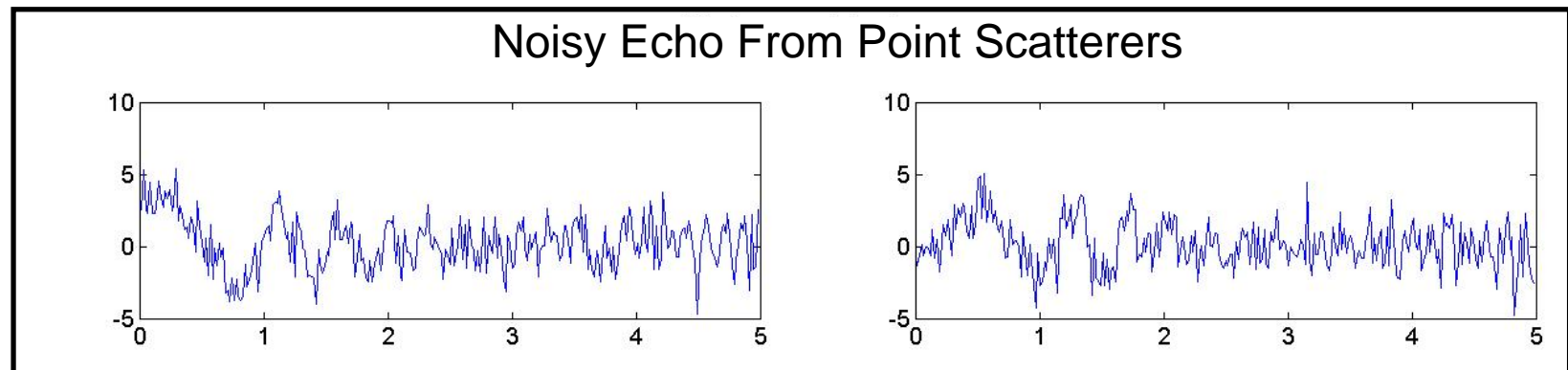
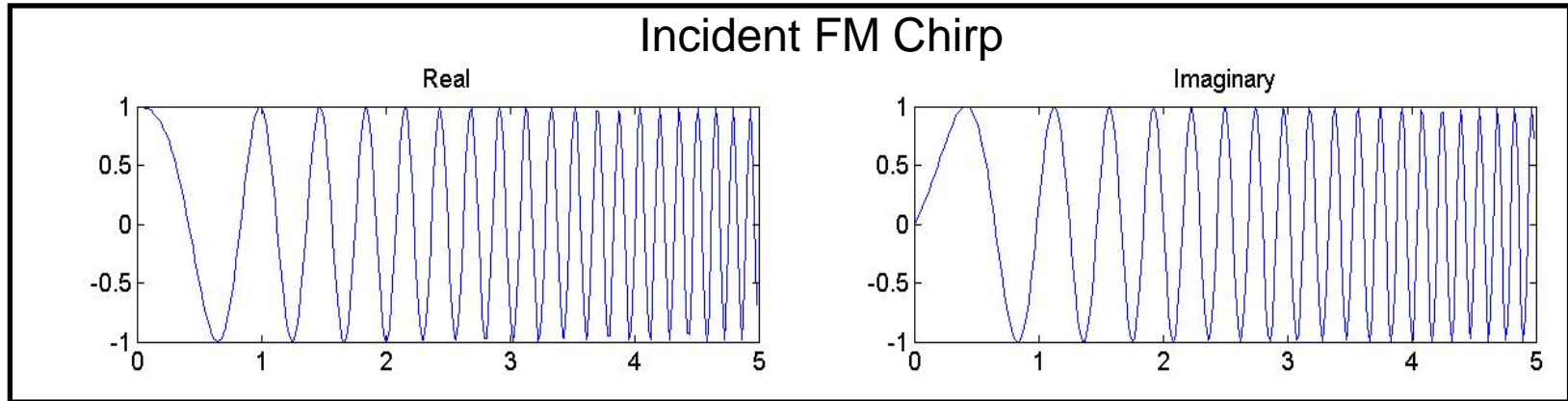
# Example For a Multi-Point Scatterer

We consider a multi-point scatterer and a linear frequency modulated (LFM) signal, or “chirp” as the probe.

The scattered signal then consists of multiple LFM signals mixed in space and time.

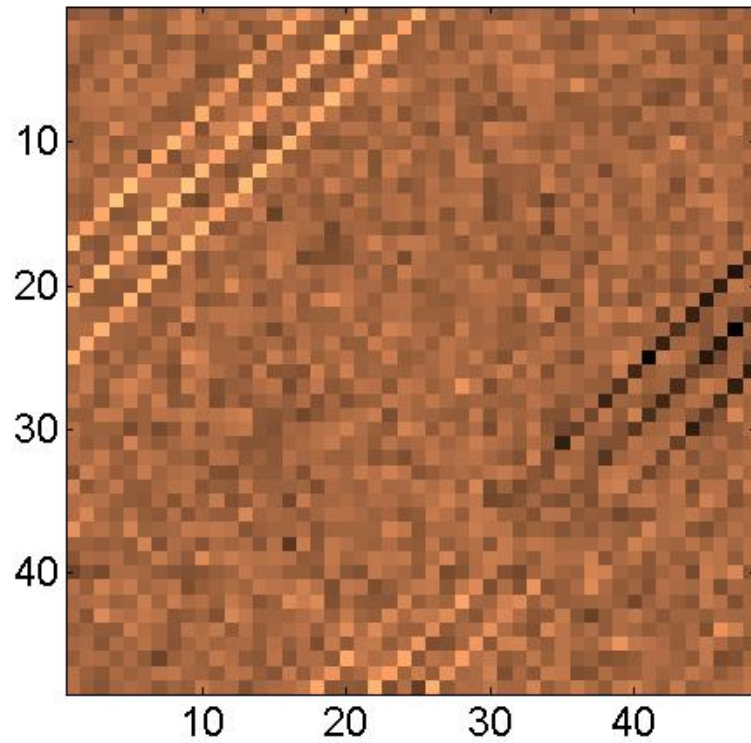


# Closely-Spaced Target Separation

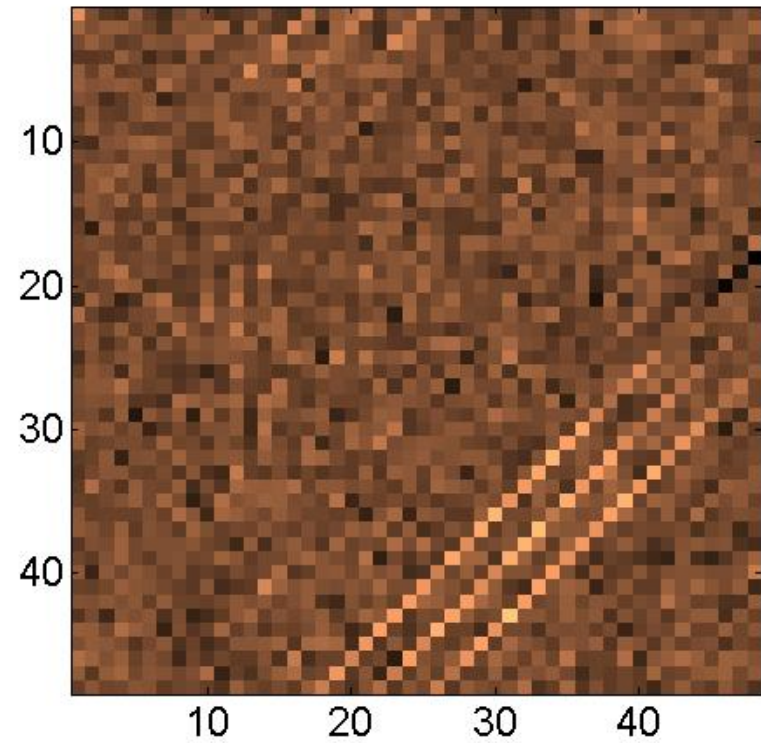


# Zak Transform of Noisy Sum

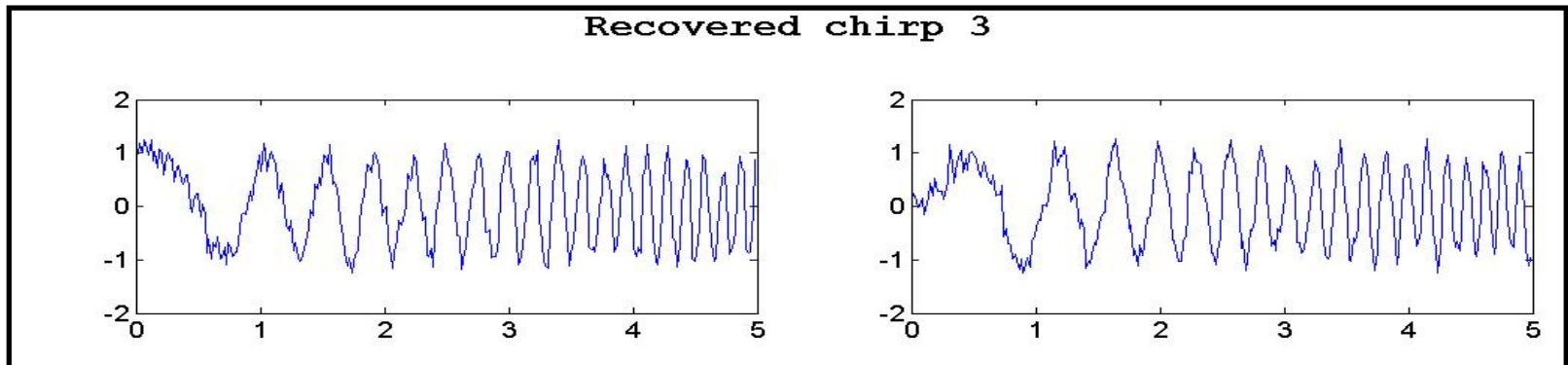
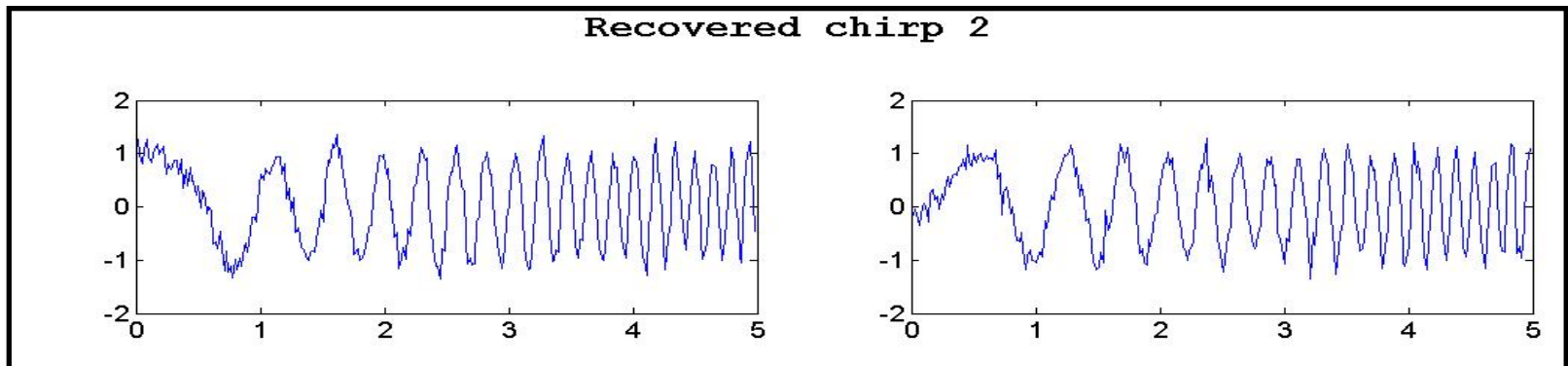
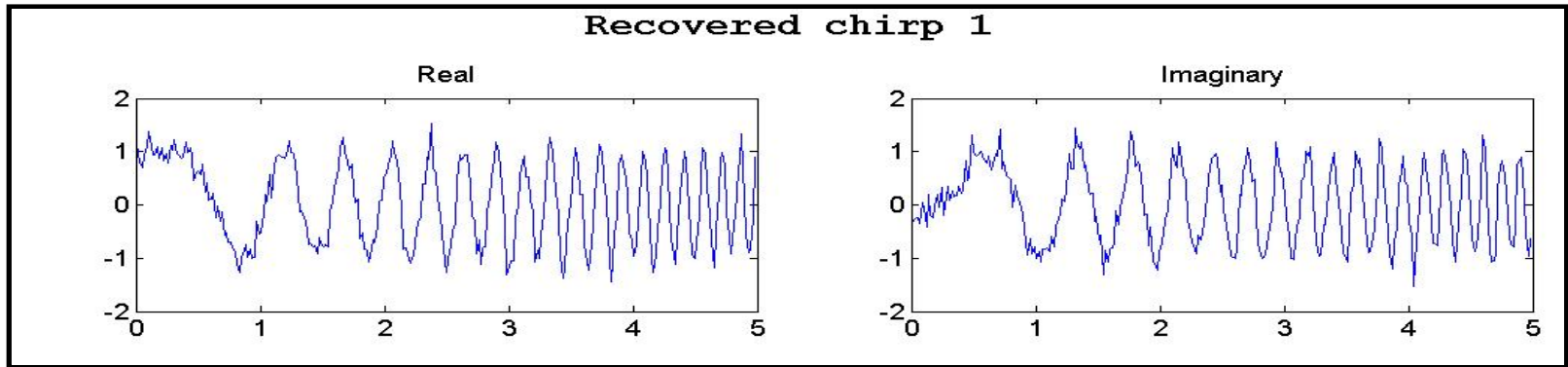
Real



Imaginary



# Recovered Decomposition



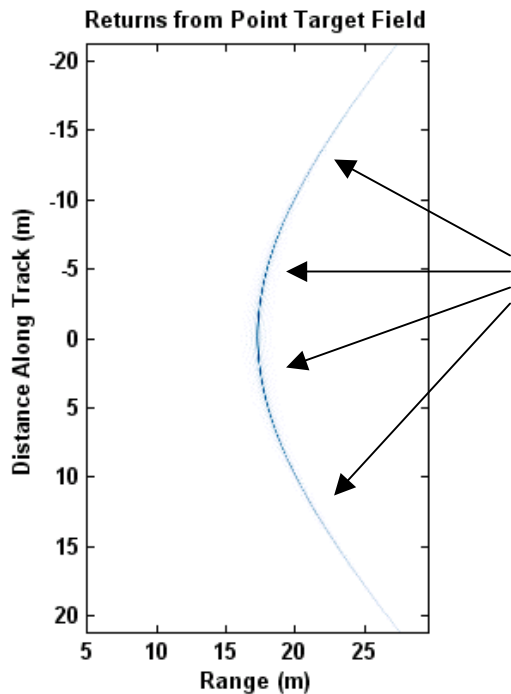


# Improving Observability with Synthetic Aperture Sonar (SAS)



# SAS: Multiple Measurements

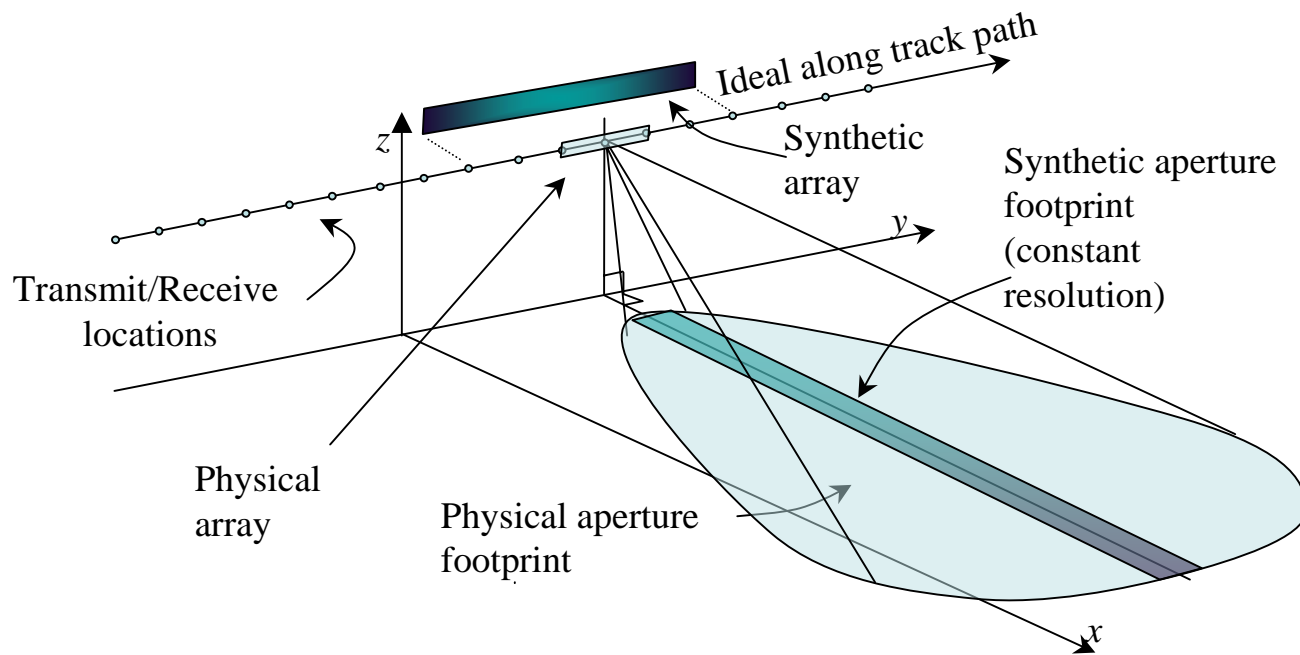
Use SAS to increase effective pulse duration by combining multiple measurements. Extends algorithm to cases where pulse duration  $<$  material relaxation time.



Multiple measurements at different aspects  
Increases cross-range resolution and observability



# SAS Geometry



# References

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